

Tenets of Static Equilibrium

(aka. Structural Zen)

- 1) sum of forces = 0 ($\Sigma F = 0$)
- 2) sum of moments = 0 ($\Sigma M = 0$)

Steps Required To Solve Statics Problems (using the Tenets of Static Equilibrium)

- 1) Draw a free-body diagram of the problem
- 2) Draw all known forces (i.e. actions)
- 3) Draw all unknown forces (i.e. reactions)
- 4) Apply the 1st tenet (sum of forces=0)
- 5) Apply the 2nd tenet (sum of moments=0)
- 6) Solve for unknown forces

(Note: Problems that can be solved with these steps are called “statically determinate”)

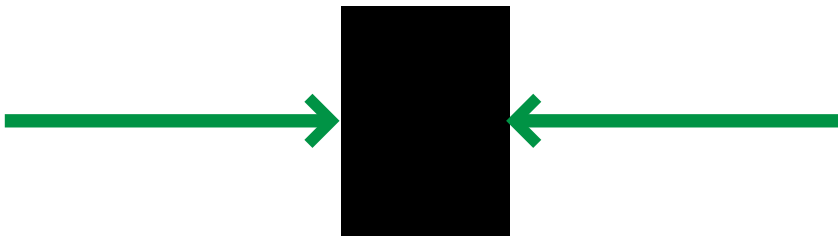
Tenets of Static Equilibrium (aka. Structural Zen)
so far just one:

1) sum of forces = 0 ($\sum F = 0$)

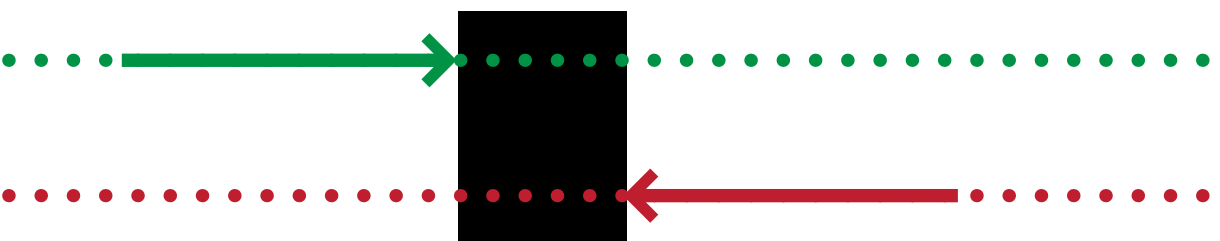
Line of Action (of a force)



So we're ok with this.



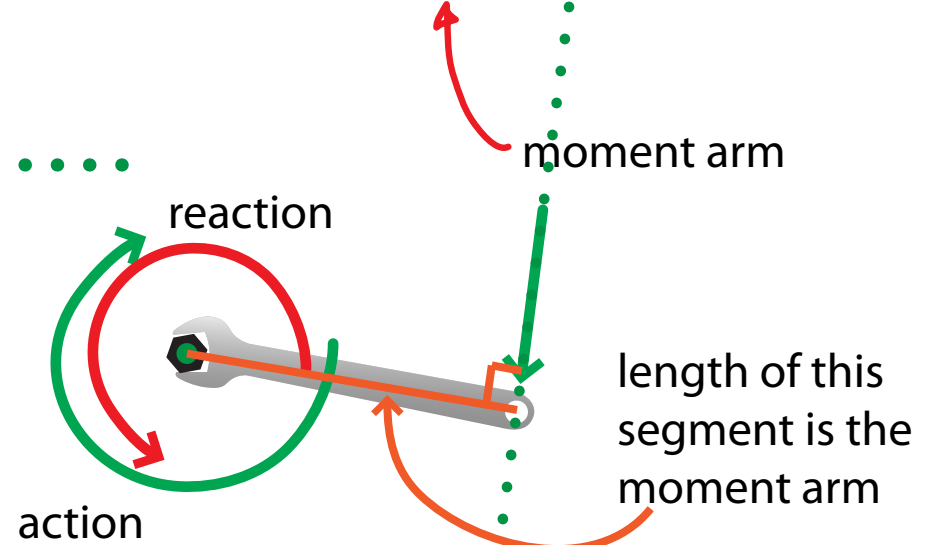
But what about this?



What happens to this object?

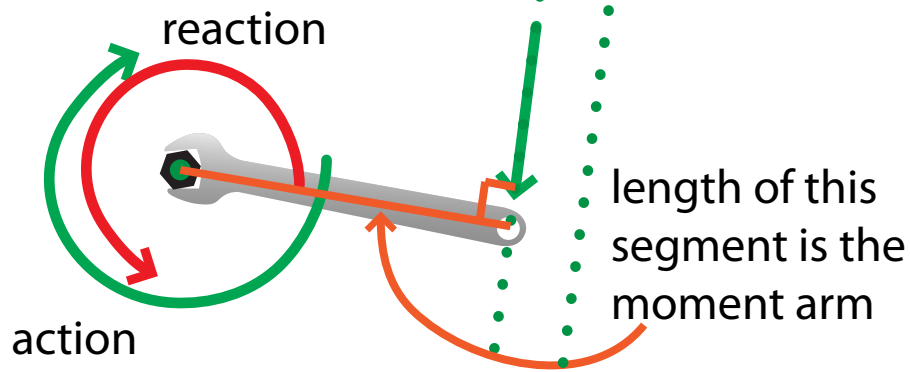
The Moment of a Force

Definition: $M = Fd$

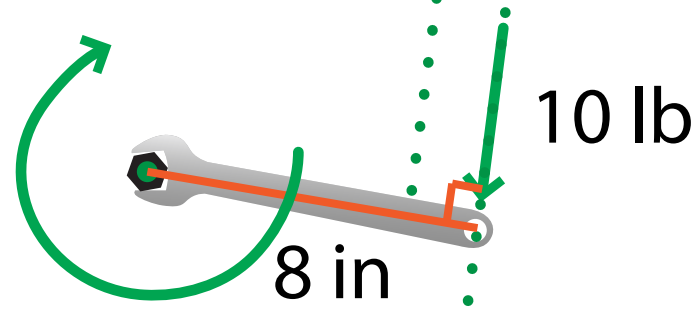


Moment of a Force needs:

- 1) a force
- 2) moment arm
- 3) point of rotation
- 4) direction of rotation
(either clockwise or counter-clockwise)



$$M = Fd = 80 \text{ in}\cdot\text{lb clockwise}$$



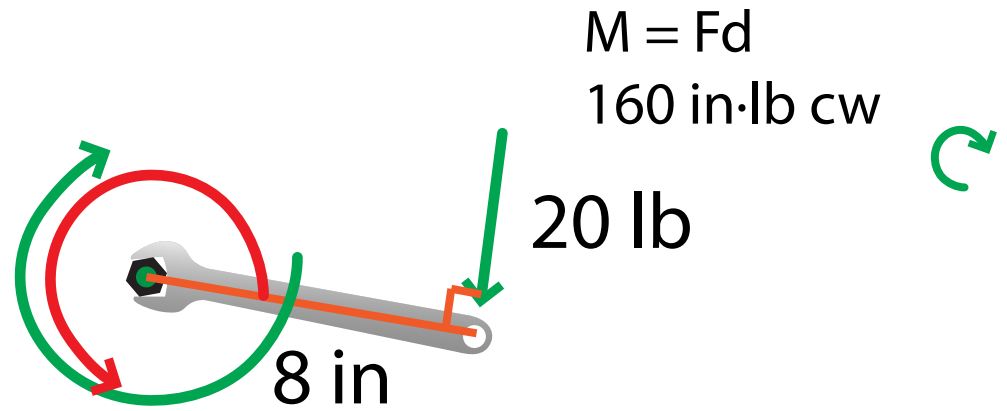
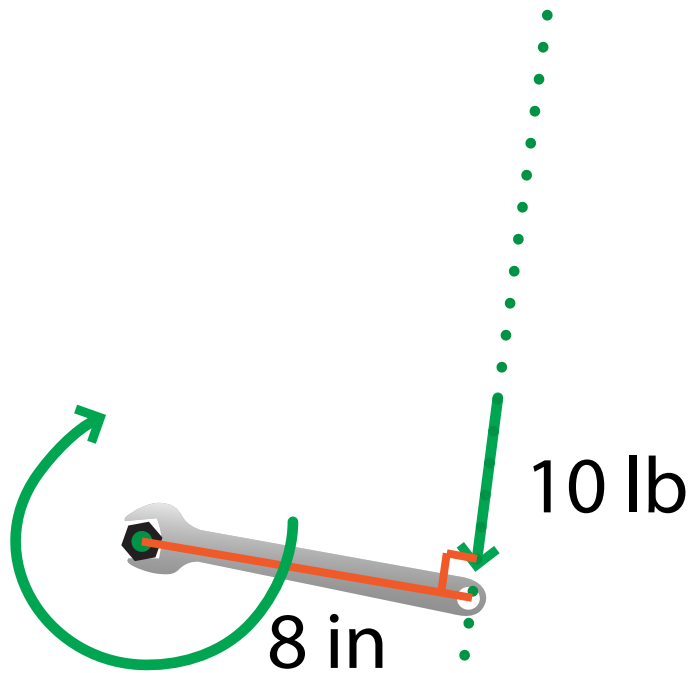
What is the moment around the bolt?

Units for moment
 in·lb (divide by 12 to get ft·lb)
 ft·lb (multiply by 12 to get in·lb)

1000 lb = 1 kip
 k·ft

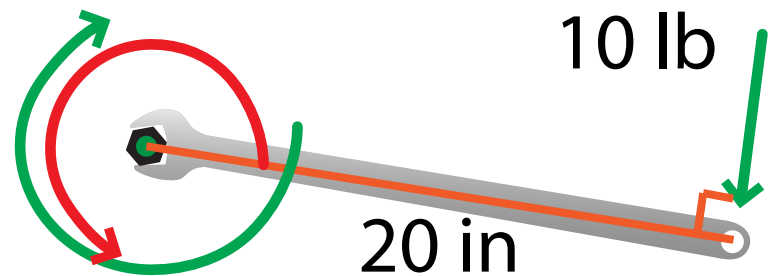
$$\Sigma F = 0 \text{ means } F + F + F + F + \dots = 0$$

$$\Sigma M = 0 \text{ means } Fd + Fd + Fd + Fd + \dots = 0$$

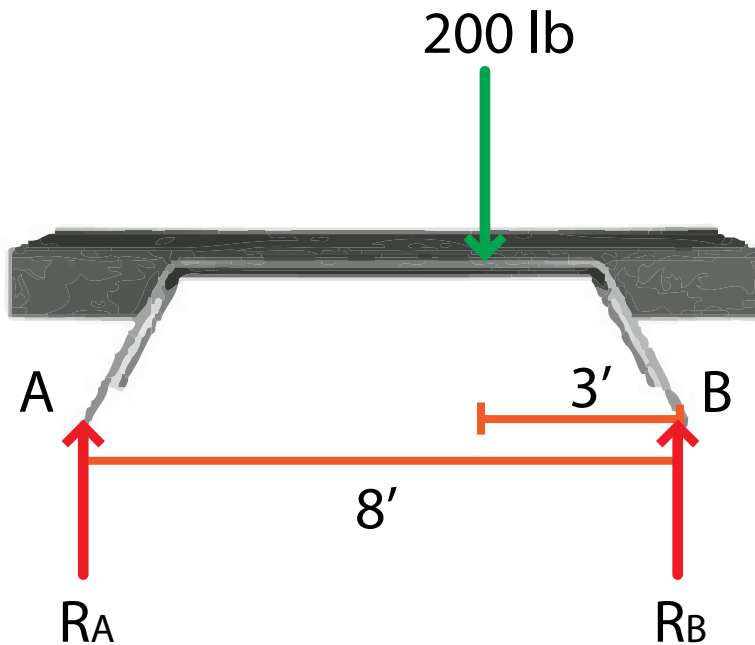


Problem: The bolt doesn't budge.
What can we do?

- 1) push harder (increase the force)
- 2) get a bigger wrench (increase the moment arm)



$$M = 200 \text{ in}\cdot\text{lb cw}$$



$$\Sigma F = 0 \quad \downarrow - \quad \uparrow +$$

$$-200 \text{ lb} + R_A + R_B = 0$$

$$\Sigma M = 0 \quad \curvearrowleft - \quad \curvearrowright +$$

1) Choose a point of rotation
If we choose B:

$$M_A = R_A(8')$$

$$M_B = R_B(0') = 0 \text{ ft}\cdot\text{lb}$$

2) Apply the equation

$$M_A + M_B + M_{DUDE} = 0$$

$$-R_A(8') + 0 + (200\#)(3') = 0$$

$$-8' \cdot R_A + 600 \text{ ft}\cdot\text{lb} = 0$$

$$-8 \text{ ft} \cdot R_A = -600 \text{ ft}\cdot\text{lb}$$

$$R_A = 75 \text{ lb up}$$

After plugging back in to the original $\Sigma F=0$ equation.

$$R_B = 125 \text{ lb up}$$